## Letter to the Editor

# Estimating the Scarlet Fever Epidemics Using a Seasonal Autoregressive Fractionally Integrated Moving Average Model\*



WANG Yong Bin<sup>1,#</sup>, XUE Chen Lu<sup>1</sup>, ZHOU Pei Ping<sup>1</sup>, ZHANG Bing Jie<sup>1</sup>, and XU Chun Jie<sup>2,#</sup>

Scarlet fever (SF) is a common infectious disease caused by *group A streptococcus* (GAS)<sup>[1]</sup>. During the 18th and 19th centuries, SF was a significant cause of mortality in children aged 5–15 years worldwide<sup>[2]</sup>. The incidence and fatality rates of SF have decreased remarkably due to the widespread use of effective antibiotics and improvements in diet and sanitation<sup>[3]</sup>. However, the recent resurgence of SF has sparked significant interest in infectious diseases<sup>[1,3]</sup>. Given the insufficient understanding of the triggers that cause SF outbreaks and the absence of available vaccines to prevent GAS infection to date<sup>[1]</sup>, effective prevention and control programs are needed to manage the ongoing spread of SF.

Time-series analysis is an invaluable tool for decision-making and strategic planning because of its ability to uncover patterns, trends, and relationships by examining and interpreting data points collected over a period<sup>[4]</sup>. Seasonal autoregressive integrated moving average (SARIMA) is the most common model in the field of health because of its straightforward structure, rapid applicability, and ability to provide meaningful insights into datasets<sup>[4]</sup>. SARIMA has proven successful in estimating the prevalence, morbidity, and mortality of contagious diseases. This is achieved by capturing temporal dependency properties and accounting for changing trends, periodic fluctuations, and random variations in a time series<sup>[4,5]</sup>. However, SARIMA fails to capture long-term temporal dependencies because it is designed to model short-term fluctuations. Moreover, the use of integer differencing in SARIMA can lead to over-differencing, potentially removing valuable information that can affect parameter estimation and fitting. Conversely, the seasonal autoregressive fractionally integrated moving average (SARFIMA), which incorporates fractional differencing into SARIMA, overcomes these limitations<sup>[6]</sup>. Thus, it is well-suited for analyzing both short- and long-term memory in time series, such as finance, economics, hydrology, and meteorology<sup>[6]</sup>. Additionally, SARFIMA does not involve complex mathematical concepts. This transparency enables end users to understand how the model is built and to depend more on the results for decision-making purposes. Despite these promising attributes, no published work has been conducted using this method to analyze and evaluate SF epidemics. Therefore, the objectives of this study were to examine the flexibility and efficacy of SARFIMA in estimating SF epidemics in Liaoning, where the yearly average morbidity was 10.363 per 100,000 persons, which is significantly higher than the average level (average, 3.26 per 100,000 people per year) in China<sup>[7]</sup>. This study also aimed to compare the predictive accuracy and reliability of SARFIMA against SARIMA.

We retrospectively gathered monthly SF incident cases and population data of Liaoning between January 2004 and December 2019 from the National Notifiable Infectious Disease Surveillance System and the Statistical Yearbook. Subsequently, the series was split into two segments: a training subset from January 2004 to December 2018 to establish the SARIMA and SARFIMA and a test subset from January to December 2019 to validate the generalization of the models. An additional testing dataset from January 2004 to December 2017 was used to determine the reliability of the models. The trend, seasonal, and irregular components were estimated using Seasonal and Trend decomposition with the Loess technique. The seasonal relative, indicating the amount by which the incidence for

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<sup>1.</sup> Department of Epidemiology and Health Statistics, School of Public Health, The First Affiliated Hospital of Xinxiang Medical University, Xinxiang 453003, Henan, China; 2. Beijing Key Laboratory of Antimicrobial Agents/Laboratory of Pharmacology, Institute of Medicinal Biotechnology, Chinese Academy of Medical Sciences & Peking Union Medical College, Beijing 100050, China

that specific time tended to be higher (or lower) than the average, was computed using multiplicative decomposition. Changing SF epidemic patterns were estimated using the average annual percentage change (AAPC) based on Joinpoint (version 4.8.0.1). SARIMA and SARFIMA were created using the "forecast" and "arfima" packages in R 4.2. Moreover, the incidence rate ratio (IRR) with a 95% confidence interval (CI) was computed in the pre- and postoutbreak SF by comparing the two proportions<sup>[2]</sup>. To determine the predictive quality, two types of measurement indicators were calculated: scaledependent metrics, such as mean absolute deviation (MAD) and root mean square error (RMSE), and metrics based on percentage errors, such as mean absolute percentage error (MAPE), mean error rate (MER), and root mean square percentage error (RMSPE)<sup>[5]</sup>. A better model was developed by minimizing these metrics.

The study included a total of 70,020 incident cases in Liaoning during 2004-2019, showing an overall increase, but no statistical significance in SF morbidity was observed, with AAPC = 4.493 (95% CI: -22.278 to 40.485; t = 0.291, P = 0.771). The highest number of 6,728 cases (15.818 per 100,000 people) was recorded in 2011, which was 2.085 times higher than the lowest number of 2,181 cases (5.142 per 100,000 people) in 2013 (Supplementary Figure S1, available www.besjournal.com). in The decomposition results indicated that the number of SF epidemics relatively increased during 2004–2010 (average 9.256 per 100,000 people annually), with an AAPC of 6.758 (95% Cl: -13.399 to 31.607; t = 0.613, P = 0.54) (Supplementary Figure S2, available in www.besjournal.com). However, an unexpected escalation was noted in 2011, and since then, it has remained relatively steady (average 11.024 per 100,000 people annually), with AAPC = 1.899 (95% CI: -12.966 to 19.302; t = 0.234, P = 0.815). SF morbidity was higher by a factor of 1.191 across the period 2004-2010 (IRR = 1.191, 95% CI: 1.188 to 1.193) (Supplementary Figures S1–S2). These results align with the SF resurgence in Hong Kong, China and South Korea<sup>[8]</sup>. However, this trend did not align with the resurgence of SF in England<sup>[2]</sup> in 2014. Moreover, the exact factors driving the increased pathogenicity of GAS are not fully understood. One probable explanation is the acquisition of novel prophages carrying new combinations of toxin and antimicrobial resistance genes. This is associated with the emergence and spread of predominant genotypes of *emm12* and *emm1* in China<sup>[3]</sup>. Another explanation could be the natural cyclic patterns of the SF. As mentioned earlier, SF epidemics in China have exhibited an approximately six-year cycle<sup>[9]</sup>. The unexpected surge since 2011 may indicate an emerging trend distinct from the previous phase of low morbidity. A third plausible reason is the relaxation of China's two-child policy in 2011, which resulted in an increase in the number of susceptible populations. Fourth, improvements in the diagnostic capacity and increased awareness among medical workers may have contributed to the observed increase. Finally, worsening air quality in China may also be a contributing factor<sup>[7]</sup>.

Remarkable semi-annual seasonality was observed in this study, with one peak in May-June and another in November-December (Supplementary Figure S3, available in www. besjournal.com). Different climatic features and the beginning of spring and autumn semesters might drive these peak activities<sup>[2,7]</sup>. Our seasonal profile concurs with the prior literature in Hong Kong, China, South Korea<sup>[8]</sup>, and China's mainland<sup>[7]</sup>. However, it disagrees with earlier findings in England (peaking in February–March)<sup>[2]</sup> and Poland (peaking in January–March)<sup>[10]</sup>. This disagreement might be attributed to differences in school breaks, population density, socioeconomic status, lifestyle, climatic and ecological features, and predominant GAS emm gene types<sup>[1,2,7]</sup>. In East Asia (including China), emm1 and emm12 are the predominant gene types responsible for SF outbreaks<sup>[3]</sup>, whereas in England, emm3, emm4, and emm12 are more prevalent<sup>[2]</sup>. These variations in gene types may contribute to differences in the timing of SF peaks between East Asia and Europe<sup>[3]</sup>. Additionally, SF epidemics remain at a low level in February each year, and some activities, such as the winter holidays and Spring Festival in China, could explain the reduced SF epidemics<sup>[7]</sup>.

The SARFIMA parameters (including p, q, P, and Q) were estimated, and the number of differencing orders and preferred modes were selected by eliminating those with a lower log-likelihood (refer to Supplementary Materials [SARFIMA method], available in www.besjournal.com). Supplementary Table S1 (available in www.besjournal.com) summarizes the modes of the best SARFIMA (3, 0, 1) $(3, -0.347, 0)_{12}$ , suggesting that the preferred model was selected as the one with mode 1. This model reported the maximum log-likelihood (-1193.7), coupled with the minimum Akaike's information criterion (2411.391) and Bayesian (2449.706). information criterion the Also, autocorrelation function (ACF) and partial ACF

results for the forecast error are provided in Supplementary Figure S4 (available in www. besjournal.com), showing most correlations were within the 95% Cl. The Ljung-Box Q test ( $\chi^2 = 0.158$ , P = 0.691) indicated no serial correlations in the residuals. These checks confirmed a white noise series of forecast errors. Similarly, based on the modeling processes, SARFIMA (2, -0.302, 1)(1, 0.471,  $2)_{12}$  was selected as the optimal model fitted to the SF incidence series during 2004-2017; the model diagnoses for their key parameters and residuals are illustrated in Supplementary Table S2 and Supplementary Figure S5 (available in www. besjournal.com). Accordingly, a prediction of the future 12 and 24 data points was achieved based on these two best SARFIMA models (Table 1 and Supplementary Table S3, available in www. besjournal.com).

Additionally, we identified the SARIMA  $(3, 0, 1)(3, 1, 0)_{12}$  and SARIMA  $(2, 1, 2)(1, 1, 2)_{12}$  specifications based on the modeling steps as the best models for the incidence series during 2004–2018 and 2004–2017, respectively (refer to Supplementary Materials [SARIMA method], Supplementary Table S4, and Supplementary Figure S6, available in www.besjournal.com). Further diagnostic checks for residuals are provided in Supplementary Figures S4–S5 and Supplementary Table S4. Figure 1 and Table 2 compare the forecasting accuracy and reliability of SARIMA and SARFIMA. The MAD, MAPE,

RMSE, RMSPE, and MER values under SARFIMA were lower than those under SARIMA for these two datasets. This indicates that SARFIMA offered a clearer perspective than SARIMA on capturing the dynamic dependency structure in the spread of SF. Previous literature has also indicated that SARFIMA is sufficient for forecasting oil supply, road fatality rate, temperature, and hemorrhagic fever with renal syndrome, and some generate more accurate results than SARIMA<sup>[6]</sup>. These studies provide additional support for our findings and reinforce the usefulness of SARFIMA as a promising alternative for analyzing SF trends and seasonality.

SARFIMA extends SARIMA, replacing the differencing term with fractional integration. With the introduction of fractional integration<sup>[6]</sup>, SARFIMA has the potential to capture long-range dependence and long memory effects in SF incidence series; it enables better capture of nonlinear patterns and complexities; it can offer more flexibility in modeling the dependence structure of SF epidemics; it can accommodate both seasonal and non-seasonal series, allowing for the modeling of multiple seasonal patterns; and it becomes robust to outliers because the inclusion of long memory helps to smooth out the effects of outliers. This explains why SARFIMA generates more accurate and flexible predictions than SARIMA. Considering the appeal of SARFIMA, the importance of this sophisticated model as a powerful forecasting tool should be

Time	Observations	SARIMA (3,	0, 1)(3, 1, 0) <sub>12</sub>	SARFIMA (3, 0, 1)(3, -0.347, 0) <sub>12</sub>		
Time	Observations	Forecasts	95% CI	Forecasts	95% CI	
January	450	397	222 to 573	416	238 to 593	
February	182	78	-171 to 327	134	-123 to 392	
March	343	206	-64 to 475	228	-48 to 505	
April	418	280	5 to 555	298	19 to 577	
May	538	594	314 to 875	540	259 to 822	
June	587	688	398 to 977	603	315 to 891	
July	380	300	2 to 598	305	8 to 602	
August	119	42	-263 to 347	99	-204 to 403	
September	217	106	-204 to 417	155	-153 to 462	
October	300	195	-119 to 509	235	-75 to 545	
November	559	505	187 to 823	488	176 to 801	
December	617	672	351 to 993	599	284 to 914	

Table 1. Forecasts between January and December 2019 using SARIMA and SARFIMA

*Note.* SARIMA, seasonal autoregressive integrated moving average; SARFIMA, seasonal autoregressive fractionally integrated moving average; *CI*, confidence interval.

underscored when analyzing the temporal levels of other communicable diseases. However, further validation is required to confirm this finding. Furthermore, several new advanced statistical techniques, such as Bayesian structural time series, flexible transmitter networks, error-trend-seasonal frameworks, and age-structure mathematical models, have recently emerged, showing potential for time series forecasting. Consequently, studies that specifically focus on comparing the predictive quality of SARFIMA with the aforementioned techniques are essential.



**Figure 1.** Comparison of the observed curves with the forecast curves under the SARIMA and SARFIMA. (A) 12 hold-out data forecasts under the SARIMA in Liaoning, (B) 12 hold-out data forecasts under the SARIMA in mainland China, (C) 12 hold-out data forecasts under the SARFIMA in Liaoning, and (D) 12 hold-out data forecasts under the SARFIMA in mainland China. The grey shaded area signifies the forecasted curve with 95% *CI* in plots. It appears that the forecasts under the SARFIMA are closer to the observed curves.

Fable 2. Comparisor	of forecast accuracy	y and reliability	under SARIMA	and SARFIMA
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Models	MAD	MAPE	RMSE	RMSPE	MER
12 hold-out data forecasts for the SF incidence	e in Liaoning				
SARIMA (3, 0, 1) (3, 1, 0) <sub>12</sub>	89.124	0.300	94.142	0.227	0.355
SARFIMA (3, 0, 1) (3, -0.347, 0) <sub>12</sub>	53.747	0.168	64.959	0.137	0.200
24 hold-out data forecasts for the SF incidence	e in Liaoning				
SARIMA (2, 1, 2) (1, 1, 2) <sub>12</sub>	133.123	0.486	153.433	0.325	0.684
SARFIMA (2, -0.302, 1) (1, 0.471, 2) <sub>12</sub>	63.199	0.239	81.777	0.154	0.384

**Note.** SARIMA, seasonal autoregressive integrated moving average; SARFIMA, seasonal autoregressive fractionally integrated moving average; MAD, mean absolute deviation; MAPE, mean absolute percentage error; RMSE, root mean square error; RMSPE, root mean square percentage error; MER, mean error rate.

This study has several limitations. First, because SF has become a milder disease with a low fatality rate since the 20th century<sup>[10]</sup>, patients with mild symptoms may not seek medical attention, leading to underreporting and underdiagnosis of SF cases. Second, owing to the unavailability of data from to 2020-2023, we only used data from 2004-2019 to indicate model performance. The COVID-19 outbreak significantly changed the SF epidemic trend from 2020-2023. Thus, the model should be regularly updated by incorporating new data to ensure reliable forecasting. Third, the findings of this study pertain specifically to how well SARFIMA estimates SF epidemics. Additional studies are needed to validate the efficiency of this method in estimating epidemics of other communicable diseases. Fourth, 100 or more observations are anticipated to be used to construct SARFIMA in applications. Finally, although SARFIMA with exogenous variables could potentially offer a higher forecasting accuracy, we could not obtain these SFrelated variables; hence, further analyses were

In summary, SARFIMA is a versatile model that can capture both short- and long-term dependencies in SF incidence as well as seasonal patterns. Its ability to capture complex dynamics and accurately forecast SF epidemics enables it to have advantages over SARIMA. Consequently, SARFIMA should be considered a valuable alternative for estimating SF epidemics to make informed decisions, optimize resources, and plan for the future. Furthermore, the incidence of SF remains high in Liaoning under current interventions. This highlights the need for additional preventive and control measures to address this evolving situation.

<sup>#</sup>Correspondence should be addressed to WANG Yong Bin, MD, Tel: 86-373-3831646, E-mail: wybwho@163.com; XU Chun Jie, Tel: 86-373-3831646, E-mail: xuchunjie@imb. pumc.edu.cn

Biographical note of the first author: WANG Yong Bin, male, born in 1989, MD, majoring in infectious disease epidemiology.

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excluded.

### Supplementary Methods

Establishing the SARIMA Usual ARIMA is specified by three components: the autoregressive (AR) component, the integrated (I) component, and the moving average (MA) component<sup>[1]</sup>, which involves predicting future epidemics based on a non-seasonal time series. The SF incidence frequently has notable seasonal effects<sup>[2]</sup>, and hence a seasonal ARIMA (SARIMA) should be adopted, it is an extension of the ARIMA by including the seasonal versions of the three components above, which is designed to capture the underlying patterns and trends by considering both the seasonal and non-seasonal components of a series<sup>[1]</sup>. The SARIMA is usually denoted as SARIMA(p, d, q)(P, D, Q)<sub>s</sub>, where p refers to the number of AR terms, d represents the degree of differencing, q signifies the number of MA terms, P, D, and Q stand for the seasonal terms above (i.e. SAR, SMA, and seasonal difference), and S is the number of periods in a season. SARIMA requires determining the six parameters above through four steps. First, SARIMA assumes stationarity, and thus stationarity of the SF incidence series was analyzed by a KPSS unit root test<sup>[3]</sup>, this statistic rejects stationarity when P < 0.05, indicating that differencing was required to achieve data stationarity, and otherwise not. Second, identifying the appropriate structure by inspecting the autocorrelation function (ACF) and partial ACF (PACF) plots that help roughly determine the values of p, q, P, and Q<sup>[4,5]</sup>. A series of combinations emerged thereof, the best one was identified by maximizing the log-likelihood (LL), and minimizing the Akaike's information criterion (AIC), corrected AIC (CAIC), and Bayesian information criterion (BIC)<sup>[1]</sup>. Third, conducting model diagnostics to judge whether the resulting residuals were white noise based on the Ljung-Box Q test, autocorrelogram, and partial autocorrelogram<sup>[1,5]</sup>. Finally, once the best model satisfied the required tests, it could be determined for forecasting purposes. Establishing the SARFIMA Time series often has a complex interplay between observed values, which is characterized by a gradual decrease in magnitude over time, following a hyperbolic decay (HD) pattern<sup>[6]</sup>. Unlike SARIMA which assumes that the autocorrelation decays exponentially, SARFIMA allows for a HD of autocorrelation, thus accommodating long-range dependence, which has been the most commonly used model to analyze the underlying mechanisms driving HD<sup>[6]</sup>. By incorporating the fractional integration ( $d_f$ ), SARFIMA provides a flexible framework for capturing both short and long memory simultaneously<sup>[6,7]</sup>.  $d_f$  in different ranges suggests various features of a series<sup>[8]</sup>. Usually, the range  $d_f \in (-1, 0.5)$  is used, so if  $d_f \in (-0.5, 0)$ , indicating the invertibility of the series; if  $d_f \in (-1, -0.5)$ , indicating the anti-persistence of the series; if  $d_f = 0$ , indicating the short memory and mean-reverting process of the series; and if  $d_f \in (0, 0.5)$ , indicating the longrange persistence of the series<sup>[6,8]</sup>. Often, a SARFIMA is denoted as SARFIMA (p, d<sup>\*</sup>, q)(P, D<sup>\*</sup>, Q)<sub>s</sub>, where d<sup>\*</sup> = d +  $d_f$  and  $D^* = D + D_f$ ,  $d_f$  or  $D_f$  represents the fractional integration, and d or D signifies the integer part (where d or  $D \ge 0$ )<sup>[6]</sup>. The Hurst (H) exponent serves as a valuable statistical measure used to analyze the long-term memory and predictability of a time series as it quantifies the degree of persistence or anti-persistence present in a series<sup>[9]</sup>. The relationship between H and d<sub>f</sub> is denoted as d<sub>f</sub> or D<sub>f</sub> = H - 0.5, so if H > 0.5, indicating a persistent

series; if H < 0.5, suggesting an anti-persistent series; and if H = 0.5, showing a random walk of series<sup>[6,7]</sup>. The computation of H includes some techniques such as rescaled range (R/S) analysis or detrended fluctuation analysis<sup>[9]</sup>. This study used the corrected R/S to determine whether the SF incidence series displays long-range properties. Constructing the SARFIMA requires selecting the best modes as it is under the assumption of multiple modes (i.e. beginning the fits with multiple starting values), causing more than one mode<sup>[6]</sup>. The best one was identified by maximizing LL and minimizing AIC and BIC<sup>[6,8]</sup>. The other steps required estimating the parameters and conducting model diagnostics, which followed what was indicated in SARIMA.

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Supplementary	Table S1.	Resultant c	andidate m	odes under	the SARFIMA(	3, 0	1)(3,	-0.347,	$(0)_{12}$

Modes	AIC	BIC	ш
Mode 1	1654.925	1690.048	-816.463
Mode 2	1656.486	1691.608	-817.243
Mode 3	1656.844	1691.967	-817.422
Mode 4	1658.588	1693.71	-818.294
Mode 5	1658.738	1693.861	-818.369
Mode 6	1659.058	1694.18	-818.529
Mode 7	1659.949	1695.072	-818.975
Mode 8	1660.268	1695.39	-819.134
Mode 9	1662.806	1697.928	-820.403
Mode 10	1663.734	1698.856	-820.867
Mode 11	1665.047	1700.17	-821.524
Mode 12	1666.785	1701.907	-822.392
Mode 13	1666.866	1701.989	-822.433
Mode 14	1667.475	1702.597	-822.737
Mode 15	1672.506	1707.629	-825.253
Mode 16	1675.773	1710.896	-826.887
Mode 17	1683.103	1718.225	-830.551
Mode 18	1692.033	1727.156	-835.017
Mode 19	1692.24	1727.362	-835.12
Mode 20	1692.442	1727.565	-835.221
Mode 21	1700.832	1735.954	-839.416
Mode 22	1702.176	1737.299	-840.088
Mode 23	1703.389	1738.512	-840.695
Mode 24	1714.219	1749.341	-846.109
Mode 25	1714.768	1749.89	-846.384
Mode 26	1732.879	1768.002	-855.44
Mode 27	1738.179	1773.301	-858.089

*Note*. SARFIMA, seasonal autoregressive fractionally integrated moving average; AIC, Akaike's information criterion; BIC, Bayesian information criterion; LL, log–likelihood.

Modes	AIC	BIC	Ц
Mode 1	1561.067	1595.431	-769.534
Mode 2	1561.444	1595.808	-769.722
Mode 3	1561.448	1595.811	-769.724
Mode 4	1561.448	1595.811	-769.724
Mode 5	1561.45	1595.814	-769.725
Mode 6	1561.486	1595.85	-769.743
Mode 7	1561.495	1595.859	-769.748
Mode 8	1561.499	1595.863	-769.75
Mode 9	1561.502	1595.865	-769.751
Mode 10	1561.506	1595.87	-769.753
Mode 11	1561.509	1595.873	-769.755
Mode 12	1561.511	1595.874	-769.755
Mode 13	1561.511	1595.875	-769.755
Mode 14	1561.512	1595.875	-769.756
Mode 15	1561.512	1595.875	-769.756
Mode 16	1561.512	1595.876	-769.756
Mode 17	1561.512	1595.876	-769.756
Mode 18	1561.514	1595.878	-769.757
Mode 19	1561.74	1596.103	-769.87
Mode 20	1561.753	1596.117	-769.877
Mode 21	1561.776	1596.14	-769.888
Mode 22	1561.791	1596.154	-769.895
Mode 23	1561.811	1596.174	-769.905
Mode 24	1561.83	1596.194	-769.915
Mode 25	1561.843	1596.207	-769.922
Mode 26	1561.846	1596.21	-769.923
Mode 27	1561.855	1596.218	-769.927
Mode 28	1561.86	1596.224	-769.93
Mode 29	1561.865	1596.229	-769.933
Mode 30	1561.867	1596.231	-769.934
Mode 31	1561.883	1596.247	-769.941
Mode 32	1561.968	1596.331	-769.984
Mode 33	1562.251	1596.615	-770.126
Mode 34	1562.261	1596.625	-770.131
Mode 35	1562.871	1597.235	-770.436
Mode 36	1563.323	1597.687	-770.661
Mode 37	1563.362	1597.726	-770.681
Mode 38	1563.447	1597.81	-770.723
Mode 39	1563.761	1598.124	-770.88
Mode 40	1564.014	1598.378	-771.007
Mode 41	1564.144	1598.507	-771.072

Supplementary Table S2. Resultant candidate modes under the SARFIMA(2, -0.302, 1)(1, 0.471, 2)<sub>12</sub>

Continued

Modes	AIC	BIC	Ш
Mode 42	1564.149	1598.512	-771.074
Mode 43	1564.15	1598.513	-771.075
Mode 44	1564.158	1598.521	-771.079
Mode 45	1564.159	1598.523	-771.08
Mode 46	1564.162	1598.526	-771.081
Mode 47	1564.189	1598.553	-771.095
Mode 48	1564.213	1598.576	-771.106
Mode 49	1564.377	1598.741	-771.189
Mode 50	1564.683	1599.047	-771.342
Mode 51	1564.755	1599.119	-771.377
Mode 52	1564.992	1599.356	-771.496
Mode 53	1565.249	1599.612	-771.624
Mode 54	1565.656	1600.02	-771.828
Mode 55	1566.507	1600.87	-772.253
Mode 56	1567.261	1601.625	-772.631
Mode 57	1567.358	1601.722	-772.679
Mode 58	1567.595	1601.959	-772.798
Mode 59	1567.683	1602.047	-772.842
Mode 60	1567.746	1602.109	-772.873
Mode 61	1568.846	1603.21	-773.423
Mode 62	1569.285	1603.649	-773.643
Mode 63	1570.262	1604.625	-774.131
Mode 64	1570.905	1605.268	-774.452
Mode 65	1570.961	1605.325	-774.481
Mode 66	1571.379	1605.742	-774.689
Mode 67	1573.295	1607.658	-775.647
Mode 68	1574.893	1609.257	-776.447
Mode 69	1575.204	1609.567	-776.602
Mode 70	1575.716	1610.079	-776.858
Mode 71	1576.168	1610.531	-777.084
Mode 72	1576.184	1610.547	-777.092
Mode 73	1576.558	1610.921	-777.279
Mode 74	1576.932	1611.296	-777.466
Mode 75	1580.158	1614.521	-779.079
Mode 76	1590.366	1624.73	-784.183
Mode 77	1590.854	1625.218	-784.427
Mode 78	1595.913	1630.276	-786.956
Mode 79	1598.18	1632.544	-788.09
Mode 80	1600.319	1634.682	-789.159
Mode 81	1611.598	1645.962	-794.799

*Note.* SARFIMA, seasonal autoregressive fractionally integrated moving average; AIC, Akaike's information criterion; BIC, Bayesian information criterion; LL, log-likelihood.

Time	Observations	SARIMA(2,	1, 2)(1, 1, 2) <sub>12</sub>	SARFIMA(2, -0.302, 1)(1, 0.471, 2) <sub>12</sub>		
Time	Observations -	Forecasts	95% CI	Forecasts	95% Cl	
18-January	638	577	408 to 746	654	471 to 837	
18-February	214	244	30 to 457	340	72 to 609	
18-March	282	328	98 to 558	423	133 to 712	
18-April	401	393	153 to 633	454	154 to 754	
18-May	797	764	510 to 1018	654	347 to 961	
18-June	855	856	575 to 1137	713	401 to 1,024	
18-July	353	571	253 to 889	441	126 to 756	
18-August	99	305	-48 to 658	219	-98 to 536	
18-September	138	305	-70 to 681	266	-53 to 585	
18-October	245	380	-9 to 769	347	27 to 667	
18-November	472	676	279 to 1,074	605	284 to 926	
18-December	631	875	467 to 1,283	709	387 to 1,030	
19-January	450	598	170 to 1,026	453	127 to 779	
19-February	182	349	-102 to 801	208	-122 to 538	
19-March	343	450	-24 to 925	308	-24 to 639	
19-April	418	442	-51 to 934	361	28 to 693	
19-May	538	730	225 to 1,235	554	221 to 887	
19-June	587	774	258 to 1,289	607	273 to 940	
19-July	380	491	-36 to 1,018	365	31 to 699	
19-August	119	287	-253 to 828	164	-170 to 498	
19-September	217	360	–197 to 918	216	–118 to 550	
19-October	300	454	-120 to 1,029	297	-37 to 631	
19-November	559	734	145 to 1,322	545	211 to 879	
19-December	617	883	283 to 1,484	629	295 to 963	

Supplementary Table S3. Forecasts between January 2018 and December 20	19 from
the SARIMA and SARFIMA	

*Note.* SARIMA, seasonal autoregressive integrated moving average; SARFIMA, seasonal autoregressive fractionally integrated moving average; *CI*, confidence interval.

Supplementary	Table S4. Identified	possible SARIMA w	vith the AIC, CAIC,	BIC, and LL values
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Madala	AIC CA1	CAIC			Ljung-Box Q test	
wodels	AIC CAIC		ыс		χ <sup>2</sup>	Р
SARIMA(3, 0, 1)(0, 1, 1) <sub>12</sub>	2012.96	2013.48	2031.70	-1000.48	0.108	0.743
SARIMA(3, 0, 1)(3, 1, 0) <sub>12</sub>	2007.61	2008.51	2032.60	-995.80	0.047	0.829
SARIMA(3, 0, 1)(2, 1, 0) <sub>12</sub>	2018.84	2019.54	2040.71	-1002.71	0.130	0.718
SARIMA(3, 0, 1)(1, 1, 0) <sub>12</sub>	2050.74	2051.26	2069.49	-1019.37	0.053	0.818
SARIMA(3, 0, 1)(1, 1, 1) <sub>12</sub>	2014.59	2015.29	2036.46	-1000.30	0.120	0.729
SARIMA(2, 0, 1)(3, 1, 0) <sub>12</sub>	2014.53	2015.23	2036.40	-1000.27	0.004	0.949
SARIMA(1, 0, 1)(3, 1, 0) <sub>12</sub>	2014.55	2015.07	2033.29	-1001.27	0.114	0.735

*Note.* SARIMA, seasonal autoregressive integrated moving average; AIC, Akaike's information criterion; CAIC, corrected Akaike's information criterion; BIC, Bayesian information criterion; LL, log-likelihood.



**Supplementary Figure S1.** Yearly incident cases and incidence rate in Liaoning during 2004–2019. This plot pinpoints that the SF outbreak occurred in 2011 and there is a periodic cycle pattern of around 4–7 years.



**Supplementary Figure S2.** A seasonal decomposition of the SF incidence series based on the STL technique. The (A) SF series is decomposed into (B) seasonal, (C) trend, and (D) irregular parts. It seems that there is a periodic outbreak pattern and a clear seasonality in SF incidence.



**Supplementary Figure S3.** The decomposed seasonal relative (SR) for the SF morbidity series using the multiplicative decomposition method. A value of SR = 1 means that the incidence for that period is exactly the same as the average. A value of SR > 1 means the incidence is higher than the average (indicating a high-risk season), and a value of SR < 1 means this period's incidence is lower than the average (indicating a low-risk season). As shown, SF epidemics present pronounced dual seasonal patterns per year.



**Supplementary Figure S4.** ACF and PACF plots for the residual series under the SARIMA and SARFIMA. (A) ACF and (B) PACF plots for the residual series under the SARIMA, (C) ACF and (D) PACF plots for the residual series under the SARFIMA. Here the correlogram demonstrates that most spikes fall within the 95% *CI* except for few outside this significance bounds (which is also reasonable because some high-order correlations easily exceed the significance bounds by chance alone), indicating that there is little evidence of non-white noise in the forecast errors.



**Supplementary Figure S5.** ACF and PACF plots for the residual series under the SARIMA and SARFIMA based on the data during 2004-2017 in Liaoning. (A) ACF and (B) PACF plots for the residual series under the SARIMA, (C) ACF and (D) PACF plots for the residual series under the SARFIMA. Here the correlogram demonstrates that most spikes fall within the 95% *CI* except for few outside this significance bounds (which is also reasonable because some high-order correlations easily exceed the significance bounds by chance alone), indicating that there is little evidence of non-white noise in the forecast errors.



**Supplementary Figure S6.** ACF and PACF plots for the seasonally differenced series in Liaoning. (A) ACF plot, and (B) PACF plot. The significant spike at lag 3 in the PACF indicates that the maximum orders may be 3 in the non-seasonal AR component, the significant spike at lag 10, 11, and 12, along with 23, 24, and 25 in the ACF suggests that the maximum orders may be 3 in the seasonal AR component. The significant spikes at lag 12, 24, and 36 in the ACF suggests that the maximum orders may be 1 in the seasonal MA component.